Evolutionary Computation

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Evolutionary Computation

Inspiring principle: theory of natural selection

"Species face the problem of searching for beneficial adaptations to the environment. The *knowledge* that each species has gained is embodied in the makeup of the chromosomes of its members." (Davis, *Genetic Algorithms and Simulated Annealing*, 1987)

Example: rabbits...

Evolutionary Computation

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Evolutionary Computation (EC) encompasses:

- Genetic Algorithms
- Genetic Programming
- Evolution Strategies
- Estimation of Distribution Algorithms

Characteristics

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- Robustness
- Adaptivity
- Subsymbolic models (no explicit symbolic computation)

Objectives

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- Problem solving
- Optimization
- Adaptive systems design
- Simulation

Some applications

- System design (e.g., airplanes, electronic circuits, mechanical elements)
- Neural network training (e.g., robotics)
- Signal processing (e.g., artificial vision)
- Optimization (discrete and continuous)

More applications

- Time series analysis and forecasting (e.g., financial forecasting)
- Artificial Life (e.g., cellular automata, analysis of complex adaptive systems)
- Games (e.g., Prisoner's Dilemma)

Challenge: find a problem where EC has NOT been applied!

Genetic Algorithms

The Metaphor

| NATURAL EVOLUTION | | ARTIFICIAL SYSTEMS |
|-------------------|-------------------|---------------------|
| Individual | \leftrightarrow | A possible solution |
| Fitness | \leftrightarrow | Quality |
| Environment | \leftrightarrow | Problem |

A bit of terminology

- A population is the set of individuals (solutions)
- Individuals are also called genotypes or chromosomes (if one solution ↔ one chromosome)
- Chromosomes are made of units called genes
- The domain of values of a gene is composed of **alleles** (e.g., a binary variable/gene has two alleles)

The Evolutionary Cycle



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Genetic operators

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- Mutation
- Recombination
- Selection
- Replacement/insertion

Genetic operators

EC algorithms define a basic computational procedure which uses the genetic operators.

The definition of the genetic operators specifies the actual algorithm.

▷ The definition of the genetic operators depends upon the problem at hand.

Genetic Algorithms

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Developed by John Holland (early '70) with the aim of:

- Understand adaptive processes of natural systems
- Design robust (software) artificial systems

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- Derived from the natural metaphor
- Very simple model
- 'Programming oriented'

You can take it as a first step toward evolutionary algorithms in general

Solutions are coded as bit strings



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Example

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Optimization of a function of integer variable $x \in [0, 100]$:

- binary coding \rightarrow string of 7 bit
- 4 bits per digit \rightarrow string of 12 bit

Genetic operators (1)

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Mutation: each gene has probability p_M of being modified ('flipped')



Genetic operators (2)

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Crossover: cross-combination of two chromosomes (loosely resembling human crossover)



Genetic operators (3)

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Selection acts in the choice of parents and produces the *mating pool*.

 \rightarrow **Proportional selection**: the probability for an individual to be chosen is proportional to its fitness.

Genetic operators (3)

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Roulette wheel



Genetic operators (4)

Generational replacement: The new generation replaces entirely the old one.

- Advantage: very simple, computationally not (extremely) expensive, easier theoretical analysis.
- Disadvantage: we could loose good solutions

High-level algorithm

Initialize Population

Evaluate Population

while Termination conditions not met do

while New population not completed do

Select two parents for mating

Apply crossover

Apply mutation to each new individual

end while

Population - New population

Evaluate Population

end while

Termination conditions

The basic question is: when to stop?

- Execution time limit reached
- We are satisfied with the solution(s) obtained
- Stagnation (limit: the population converged to the same individual)

```
Initialize Population {N_{pop} individuals X_1, \ldots, X_{N_{pop}}}
for i = 1 to N_{pop} do
X_i \leftarrow InitialSolution() {e.g., random}
end for
```

Evaluate Population{Individual X_i has fitness F_i } for i = 1 to N_{pop} do $F_i \leftarrow \text{Eval}(X_i)$ end for

```
Select parents: G_1, G_2{Roulette wheel selection}

lung \leftarrow 0

for i = 1 to N_{pop} do {all fitness values are summed up}

lung \leftarrow lung + F_i

end for

for m = 1 to 2 do

r \leftarrow \text{Random}(0, lung); sum \leftarrow 0; i \leftarrow 1

while i < N_{pop} AND sum < r do

sum \leftarrow sum + F_i; i \leftarrow i + 1

end while

G_m \leftarrow X_i

end for
```

Apply crossover: from G_1, G_2 we get G'_1, G'_2 $r \leftarrow \text{Random}(1, I_{chromosome}) \{\text{crossover point}\}$ for i = 1 to r - 1 do $G'_1[i] \leftarrow G_1[i]$ $G'_2[i] \leftarrow G_2[i]$ end for for i = r to $I_{chromosome}$ do $G'_1[i] \leftarrow G_2[i]$ $G'_2[i] \leftarrow G_1[i]$ $G'_2[i] \leftarrow G_1[i]$

end for

Apply mutation to individual X for i = 1 to $l_{chromosome}$ do $r \leftarrow \text{Random}(0,1)$ if $r \leq p_M$ then Complement X[i]end if end for

Fitness Landscape

Representation of the space of all possible genotypes, along with their fitness.



Fitness Landscape

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Caution!

- Different landscapes for different operators
- In many cases fitness landscapes are dynamic
- Landscape 'intuition' might be misleading
- Use of term local optimum used and abused everywhere

Why does it work?

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Intuition:

- Crossover combines good parts from good solutions (but it might also destroy... sometimes)
- Mutation introduces diversity
- Selection drives the population toward high fitness

Why does it work?

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Holland explains (also theoretically, but with strong hypotheses) why the SGA 'works'

Two basic elements:

- Schemata
- Building blocks

Schemata

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- A schema is a kind of mask: 001 * 1 * *0
- The symbol * represents a wildcard: both 0 and 1 fit
- E.g., 1 * 0 represents 100 and 110

Building blocks

- A building block is a pattern of contiguous bits
- HP: good solutions are composed of good building blocks
- The crossover puts together short building blocks and destroys large ones

Implicit parallelism

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- · Every individual corresponds to a set of schemata
- The number of the best schemata increases exponentially
- The solution space is searched through schemata (hence implicit parallelism)

When does it work well?

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A SGA works well if:

- 1 Short good building blocks (correlate genes are adjacent)
- 2 Loose interaction among genes (low epistasis)

SGA: pros and cons

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Pros:

- Extremely simple
- General purpose
- Theoretical models

Cons:

- Coding
- Too simple genetic operators

A recipe

The ingredients to prepare a GA:

- Solution coding (e.g., bit strings, programs, arrays of real variables, etc.)
- Define a way of evaluating solutions (e.g., objective function value, result of a program, behavior of a system, etc.)
- Define recombination operators (crossover, mutation)
- Define the selection and replacement/insertion mechanisms

Toward less simple GA

Recombination:

- *Multi-point crossover* (recombination of more than 2 "pieces" of chromosomes)
- *Multi-parent crossover* (an individual is generated by more than 2 parents)
- Uniform crossover (children created by randomly shuffling the parent variables at each site)

Multi-point crossover



Multi-parent crossover



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Toward less simple GA

Mutation:

- Learning applied to modify the chromosome
- In optimization, hill-climbing or more complex local search algorithms can be applied

Interesting topic: Evolution & Learning,

www.cogs.susx.ac.uk/users/ezequiel/alife-page/evolearn.html

Toward less simple GA

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Selection:

- Different probability distribution (e.g., probability distribution based on the *ranking* of individuals)
- *Tournament Selection* (iteratively pick two or more individuals and put in the *mating pool* the fittest)

Ex: real valued variables

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- Solution: $x \in [a, b], a, b \in \mathbb{R}$
- Mutation: random perturbation $x \rightarrow x \pm \delta$, accepted if $x \pm \delta \in [a, b]$
- Crossover: linear combination z = λ₁x + λ₂y, with λ₁, λ₂ such that a ≤ z ≤ b.

Example: permutations

- Solution: *x* = (*x*₁, *x*₂,..., *x_n*) is a permutation of (1,2,..., *n*)
- Mutation: random exchange of two elements in the *n*-ple
- Crossover: like 2-point crossover, but avoiding value repetition (see next example).

Eight Queens



Place 8 queens on a 8 \times 8 chessboard in such a way that the queens cannot attack each other.



Genotype: a permutation of the numbers 1 through 8





Mutation: exchanging two numbers





Eight Queens

Crossover: combining two parents





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Fitness: penalty of a queen is the number of queens it can check.

The fitness of the configuration is the sum of the single penalties.

Genetic Programming

- Can be seen as a 'variant' of GA: individuals are programs
- Used to build programs that solve the problem at hand (⇒ specialized programs)
- Extended to *automatic design* in general (e.g., controllers and electronic circuits)

Genetic Programming

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Individuals are trees which encode programs.



Fitness given by the evaluation of the program "behavior" (based upon some defined criteria)

Operators

Mutation: Random selection of a subtree which is substituted by a *well formed* random generated subtree



Operators

Crossover: Exchange two randomly picked subtrees.



Operators

Selection and replacement

Fitness is evaluated depending on the application.

- For assembler worms the fitness can be the memory they occupied.
- For controllers, the fitness can be the percentage of correct actions

The realm of GP

- Black art problems. E.g., automated synthesis of analog electrical circuits, controllers, antennas, and other areas of design
- Programming the unprogrammable, involving the automatic creation of computer programs for unconventional computing devices. E.g.,cellular automata, parallel systems, multi-agent systems, etc.

Coevolution

Species evolve in the same environment

\rightarrow *dynamic* environment

Two kinds:

- Competitive
- Cooperative

Competitive Coevolution

> Species evolve trying to face each other

• E.g., prey/predator, herbivore/plants.

Applications: ALU design for Cray computer, (pseudo-)random number generator.

Cooperative Coevolution

 \triangleright Species evolve complementary capabilities to survive in their environment

• E.g., host/parasite.

Applications: 'niche' genetic algorithms for *multi-criteria* optimization.

EC and Artificial Life

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Tierra

- Artificial evolution of computer programs (T. Ray, early '90s)
- Environment: virtual computer
- Individuals: self-replicating assembler programs
- Resources: CPU time and memory

Tierra

Results of evolution: several kinds of nontrivial behaviors and dynamics

- parasites
- immunity to parasites
- circumvention of immunity to parasites
- social individuals
- ... and others

EC and Games

Axelrod and The Prisoner's Dilemma

- Game strategies evolved through genetic algorithms
- Dynamic environment (a player plays against other different players)
- Best strategy evolved by GA is the best human strategy
- Analysis of the arising of cooperation

The Prisoner's Dilemma

- The two players in the game can choose between two moves, either *cooperate* or *defect*.
- Each player gains when both cooperate, but if only one of them cooperates, the other one, who defects, will gain more.
- If both defect, both lose (or gain very little) but not as much as the "cheated" cooperator whose cooperation is not returned.

The payoff matrix

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| Action of $A \setminus Action$ of B | Cooperate | Defect |
|---------------------------------------|-----------|--------|
| Cooperate | +5 | -10 |
| Defect | +10 | 0 |

Problem encoding

Suppose that the memory of each player is one previous move. E.g., player A cooperated and player B defected becomes: CD.

The strategy is defined with a move for each possible past move. E.g.:

- If CC then C
- If CD then D
- If DC then C

 \rightarrow the string is CDCD

If DD then D

Classifier Systems

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Systems composed of rules like

IF [conditions] THEN [actions]

IF (sensor1 is active) THEN (move)
IF (sensor3 is inactive and sensor4 is active) THEN (stop)
IF (sensor4 is inactive) THEN (turn right)

Rules are usually coded as bitstrings and evolved by means of usual application of EC operators.

Classifier Systems



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Classifier Systems



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